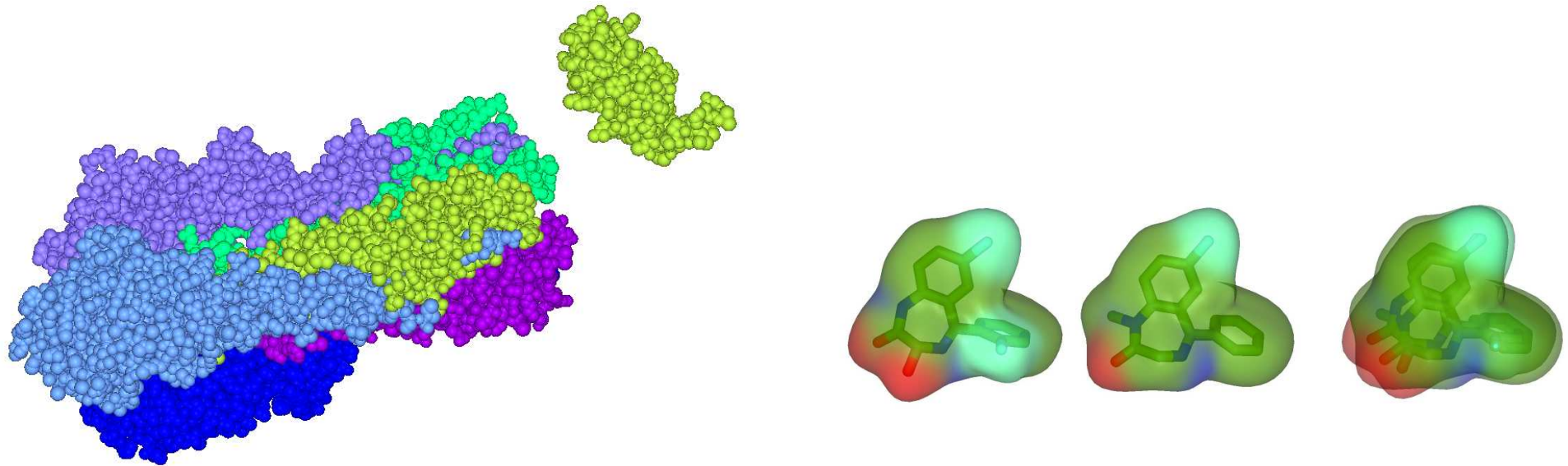


# Protein Docking and 3D Ligand-Based Virtual Screening

## Part 2



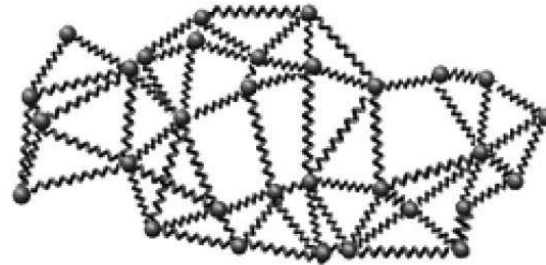
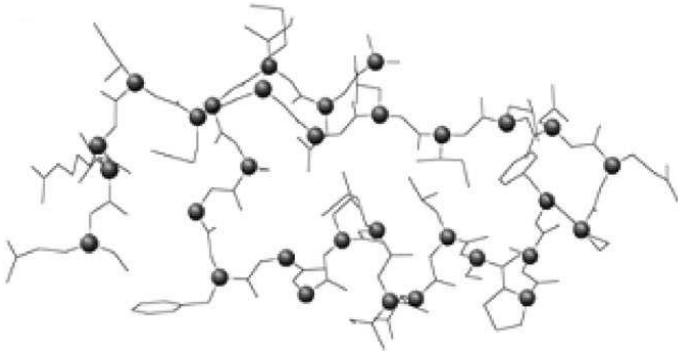
Dave Ritchie

Orpailleur Team

INRIA Nancy – Grand Est

# Modeling Protein Flexibility Using Elastic Network Models

- ENMs assume protein atoms (often just CAs) are coupled via a harmonic potential:



$$V = \sum_{i < j} C (d_{ij} - d_{ij}^0)^2$$
$$H_{ij} = (\partial / \partial x_i) (\partial / \partial x_j) V$$
$$\underline{H} = \underline{E}^T \cdot \underline{\Lambda} \cdot \underline{E}$$

- $C$  = constant,  $d_{ij}$  = distance,  $d_{ij}^0$  = reference distances,  $V$  = potential,  $\underline{H}$  = Hessian
- $\underline{E}$  = matrix of eigenvectors  $\underline{e}_i$  (normal mode “directions”),  $\Lambda_{ii}$  = eigenvalues (magnitudes)
- Then, sort by eigenvalues, and represent protein conformations as linear combinations

$$\underline{P}^{NEW} = \underline{P}^0 + \sum_{i=6}^{3N} w_i \underline{e}_i$$

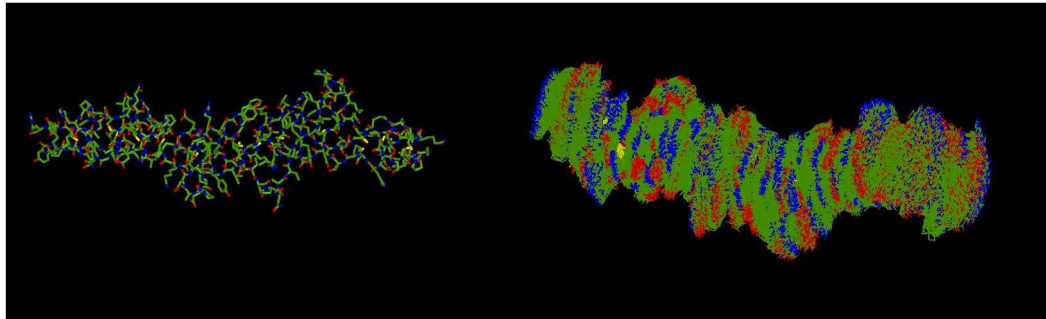
- On-line examples: <http://www.igs.cnrs-mrs.fr/elnemo/>, and <http://www.molmovdb.org/>
- Problem #1: how to find weights  $w_i$  to give protein conformation  $\underline{P}^{BOUND} = \underline{P}^{NEW}$  ?
- Problem #2: How to sample and combine conformations for two proteins ?

[Andrusier et al. \(2008\), Proteins, 73, 271–289 \(recent review on flexible docking\)](#)

[Tirion \(1996\) Physical Review Letters, 77, 1905–1908 \(original ENM article\)](#)

# Simulating Flexibility During Docking using “Essential Dynamics”

- Generate distance-constrained samples in CONCOORD, then apply PCA



- Covariance matrix,  $C$ :

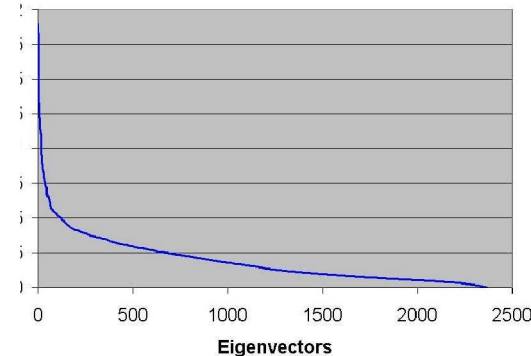
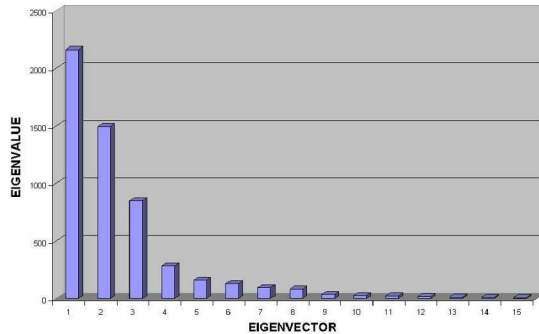
$$C_{ij} = \langle (x_i - \bar{x}_i)(x_j - \bar{x}_j) \rangle$$

- Calculate eigenvectors,  $E$ :

$$\underline{C} = \underline{E} \cdot \underline{\Lambda} \cdot \underline{E}^T$$

- Estimate Unbound to Bound:

$$\underline{B} \simeq \underline{U} + \sum_{k=1}^n \alpha_k \underline{e}_k$$



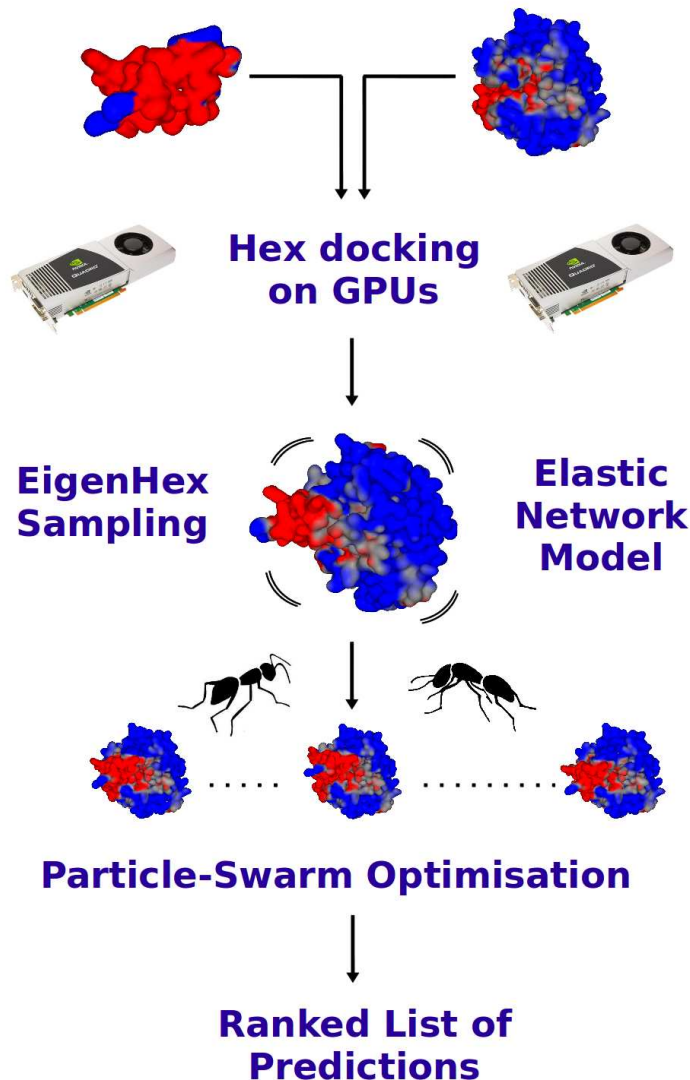
- The first few eigenvectors encode most of the internal fluctuations
- See also SwarmDock – <http://bmm.cancerresearchuk.org/~SwarmDock/>

Mustard, Ritchie (2005), *Proteins* 60, 269–274 (first NMA protein docking?)

Moal, Bates (2010) *Int J Molecular Sciences*, 11, 3623–3648 (SwarmDock)

# EigenHex – Flexible Docking Using Pose-Dependent ENM

- Apply fresh eigenvector analysis to the top 1,000 Hex orientations



## Overall approach

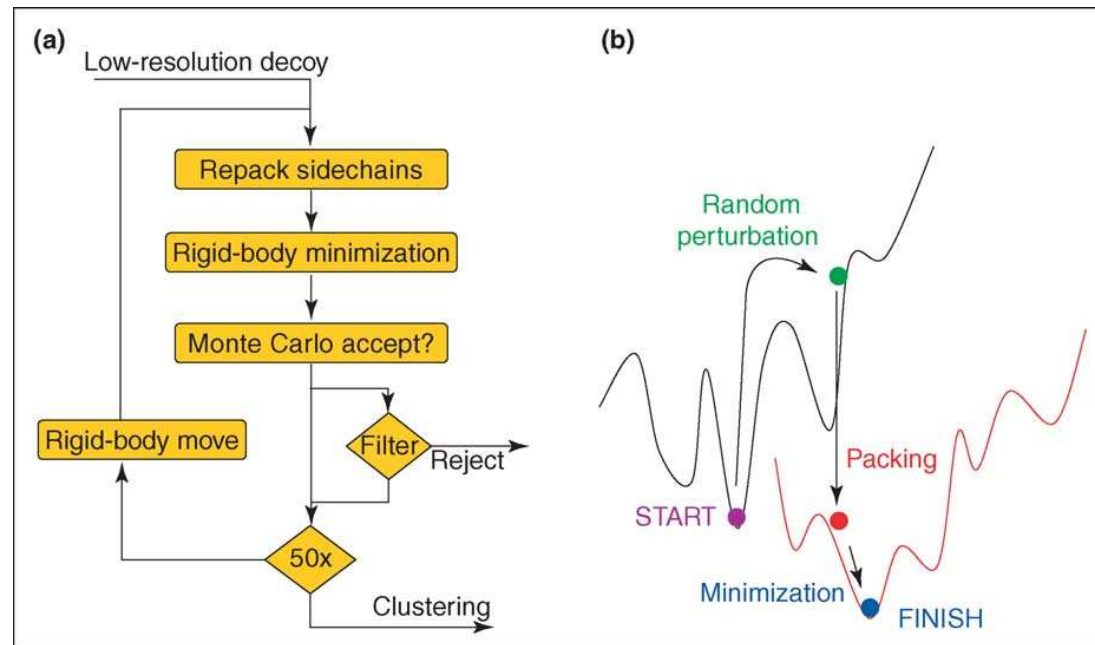
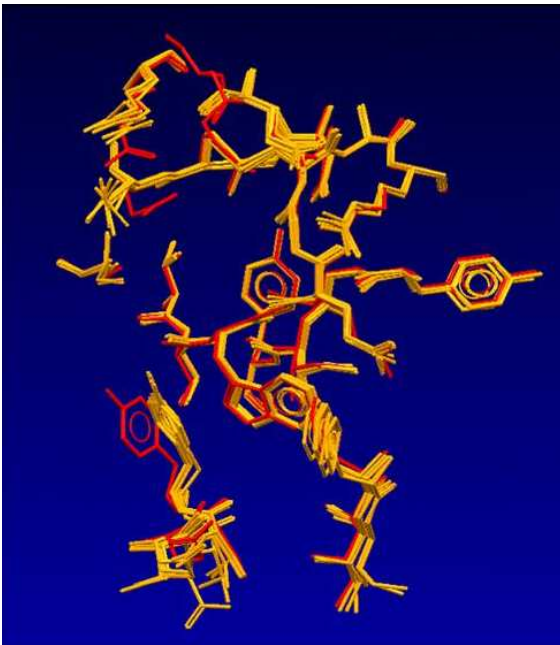
- $C\alpha$  elastic network model (ENM)
- Use up to 20 eivenvectors
- Search using PSO
- Score using “DARS” potential

## Results

- DARS potential works well but...
- Still need a better scoring function
- Much effort – small improvement !!

# RosettaDock – Flexible Refinement by Side Chain Re-Packing

- Given a rigid body starting pose, repeat 50 times:
  - REMOVE and RE-BUILD side chains; apply local rigid-body minimisation
  - apply Monte-Carlo accept/reject



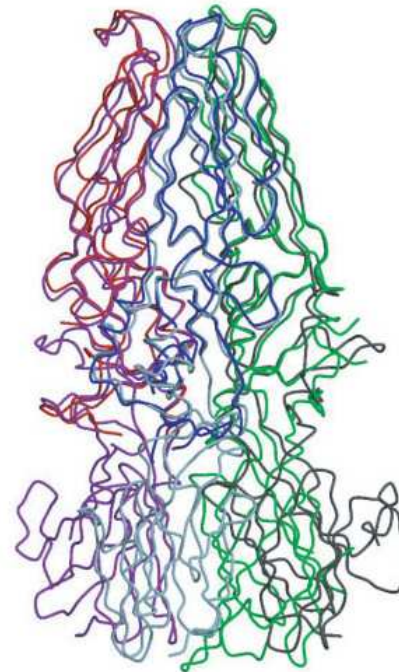
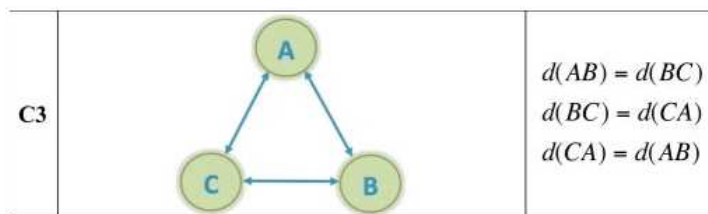
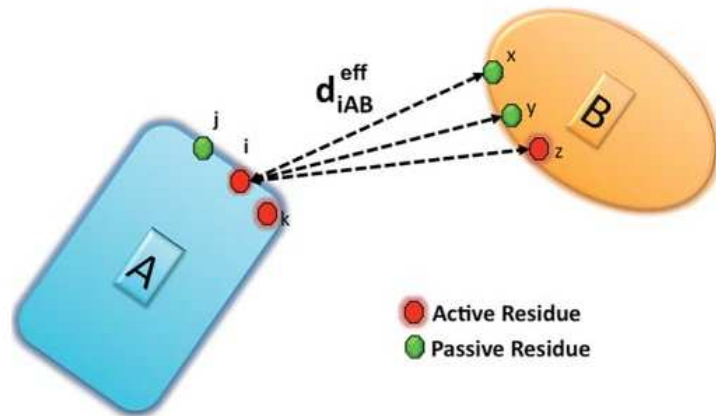
- Successful for several CAPRI targets; also works well for 50% of Docking Benchmark v2

Gray (2006) *Current Opinion in Structural Biology*, 16, 183–193

# Haddock – “Highly Ambiguous Data-Driven Docking”

- Flexible refinement using CNS with ambiguous interaction restraints (AIRs)
- Use of “active” and “passive” residues ensures active residues at interface

- E.g. residue  $i$  of protein A: 
$$d_{iAB}^{\text{eff}} = \left( \sum_{m_{iA}=1}^{N_{iA}} \sum_{k=1}^{N_{\text{res}B}} \sum_{n_{kB}=1}^{N_{kB}} \left( \frac{1}{d_{m_{iA},n_{kB}}^6} \right) \right)^{-1/6}$$



T10 = TEV trimer

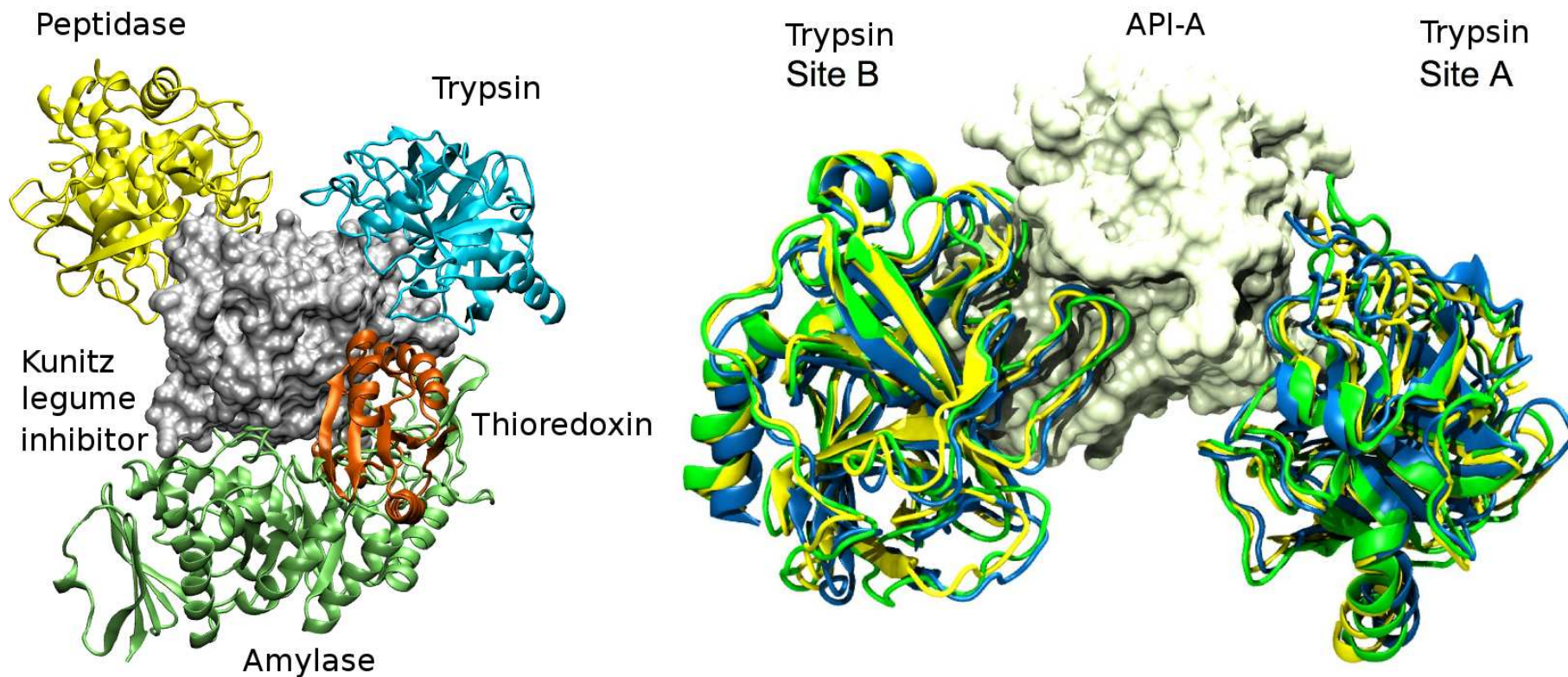
- V. good CAPRI results
- Restraints from (e.g.):  
 SAXS  
 mutagenesis  
 mass spectroscopy  
 NMR (RDC, CSP)

van Dijk et al. (2005) FEBS J, 272, 293–312

van Dijk et al. (2005) Proteins, 60, 232–238

# Knowledge-Based Protein Docking: CAPRI Target 40 (2009) – API-A/Trypsin

- We searched SCOPPI and 3DID for similar domain interactions to the target
- This helped to identify two key inhibitory loops on API-A around L87 and K145

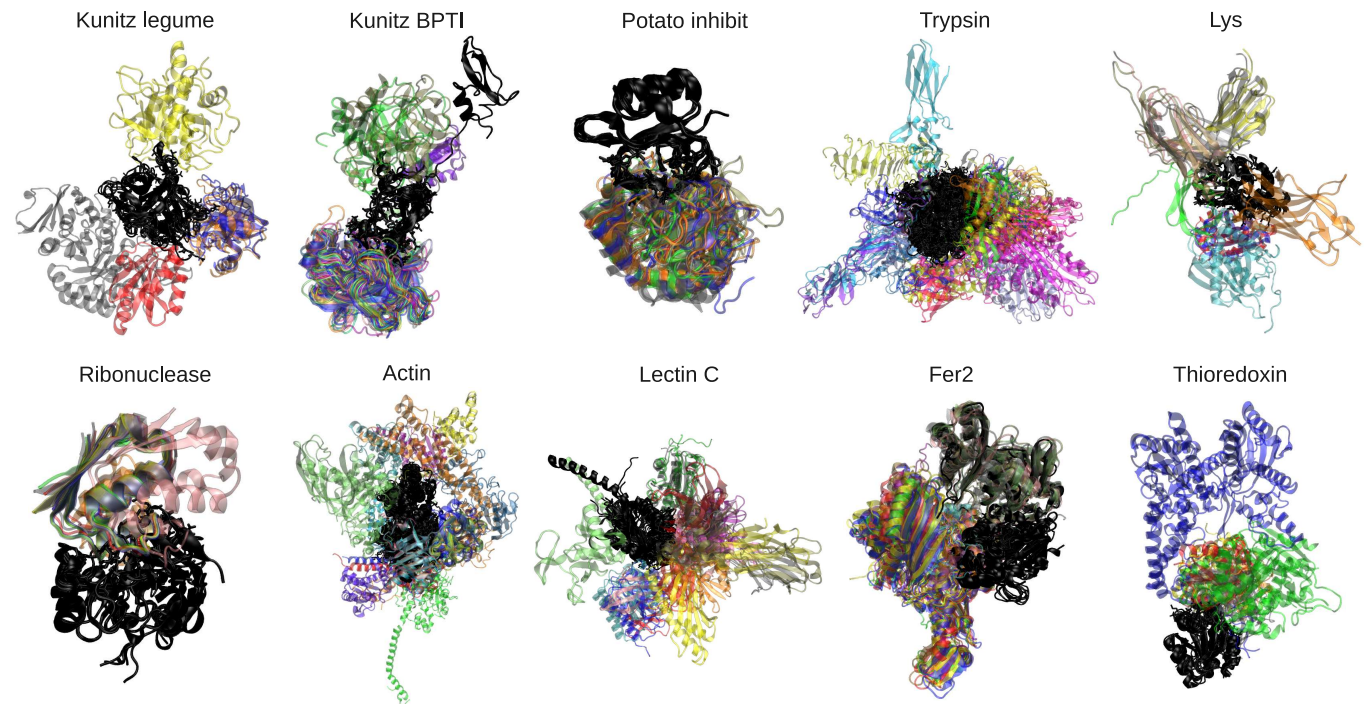
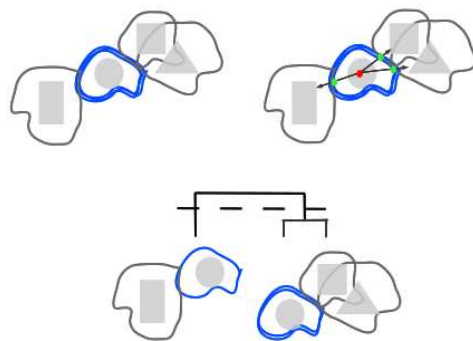
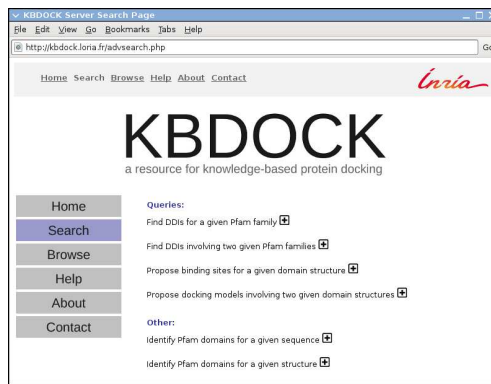


- Performing focused Hex + MD refinement gave a total of 9 “acceptable” solutions

# The KBDOCK Database and Web Server

- Content: 2,721 non-redundant hetero DDIs involving 1,029 PFAM domain families
- For each PFAM family, all DDIs are superposed and spatially clustered

<http://kbdock.loria.fr/>

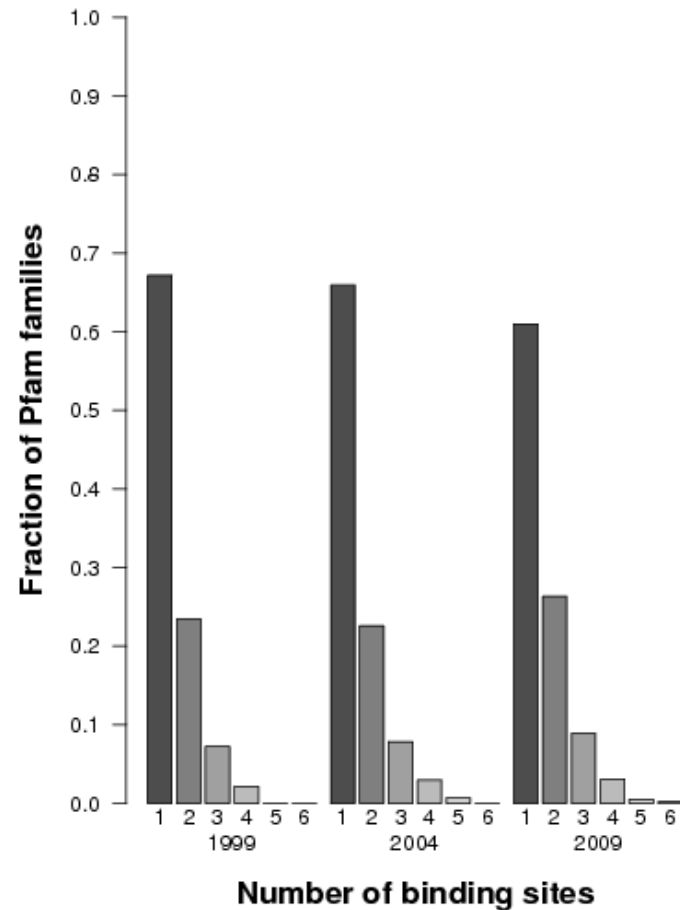
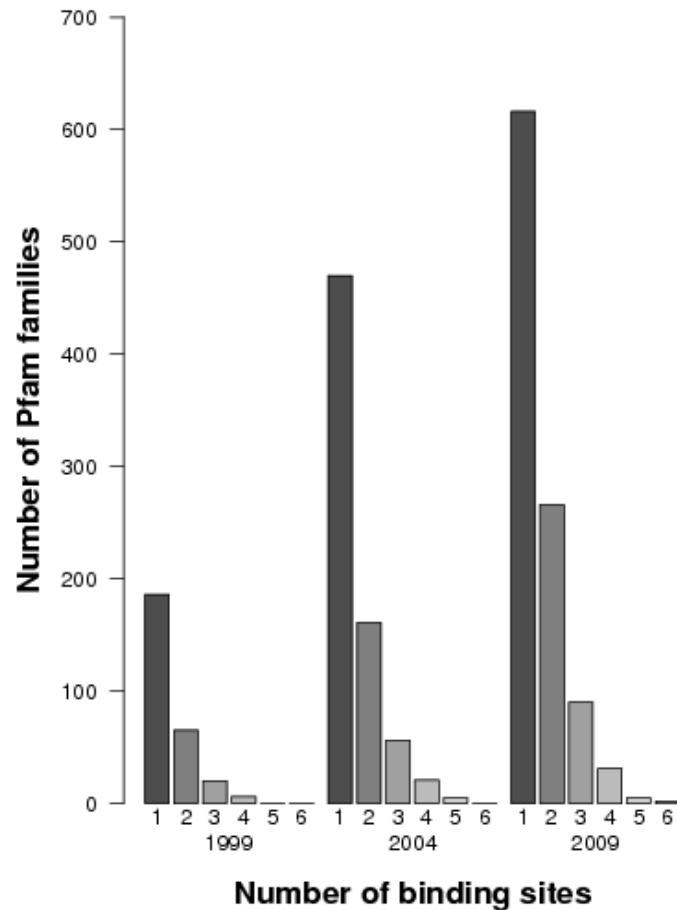


- Aim: to provide PFAM family-level structural templates for knowledge-based docking



# KBDOCK – Analysis of PFAM Domain Family Binding Sites

- Nearly 70% of PFAM domain families have just one binding site
- Very few domains have more than two or three binding sites



- This supports the notion that protein binding sites are often re-used...

# KBDOCK – Template-Based Protein Docking Results

- The Protein Docking Benchmark 4.0 contains 176 protein-protein complexes
- We selected 73 single-domain complexes
- A “Full-Homology” (FH) template matches both target domains
- A “Semi-Homology” (SH) template matches just one target domain

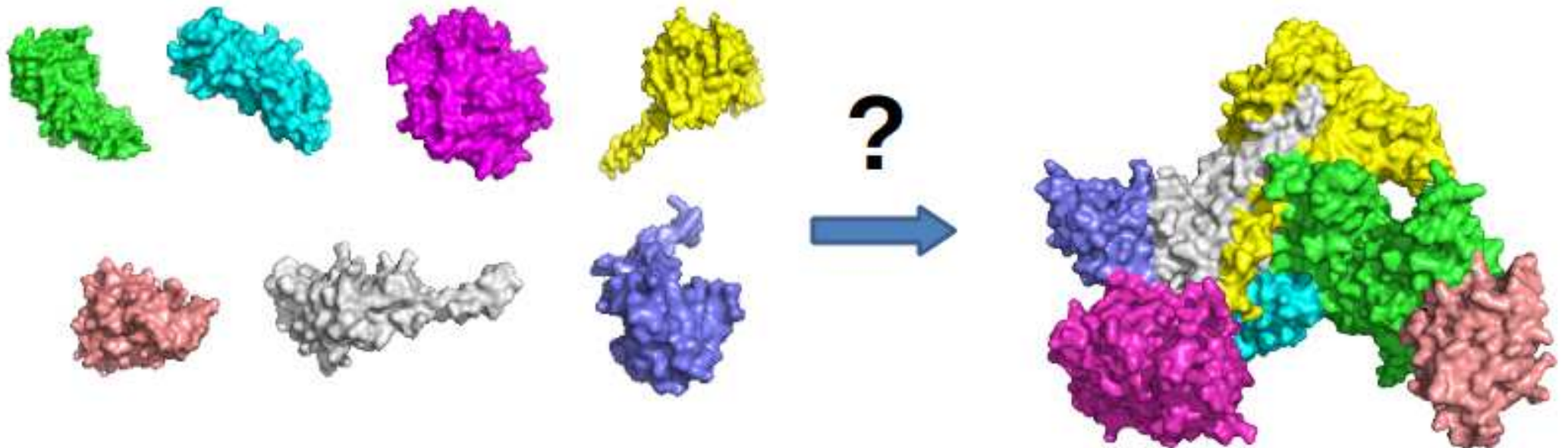
| Target class                  | Total targets | FH templates | Two SH templates | One SH template | Zero templates |
|-------------------------------|---------------|--------------|------------------|-----------------|----------------|
| <b>Without date filtering</b> |               |              |                  |                 |                |
| Enzyme                        | 36            | 24 / 24      | (3 + 1) / 5      | 3 / 5           | 2              |
| Other                         | 37            | 21 / 21      | (0 + 0) / 3      | 5 / 11          | 2              |
| <b>With date filtering</b>    |               |              |                  |                 |                |
| Enzyme                        | 36            | 13 / 13      | (2 + 1) / 5      | 7 / 11          | 7              |
| Other                         | 37            | 13 / 13      | (0 + 0) / 1      | 8 / 15          | 8              |

- If a FH template exists, it is almost always correct
- Even if there is no FH template, SH templates can still provide useful information

Ghoorah et al. (2011), *Bioinformatics*, 27, 2820–2827

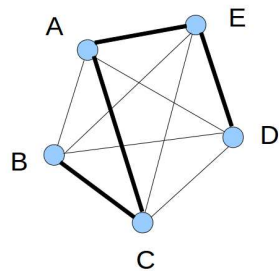
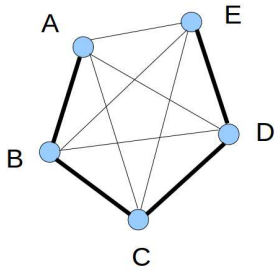
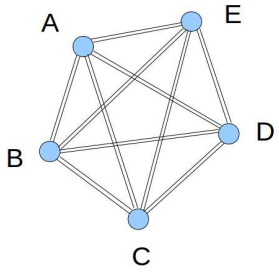
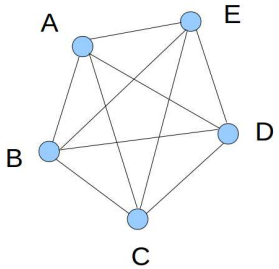
# Assembling Multi-Component Protein Complexes

- Multi-component assembly is a highly combinatorial problem
- How to generate and score candidate orientations efficiently?



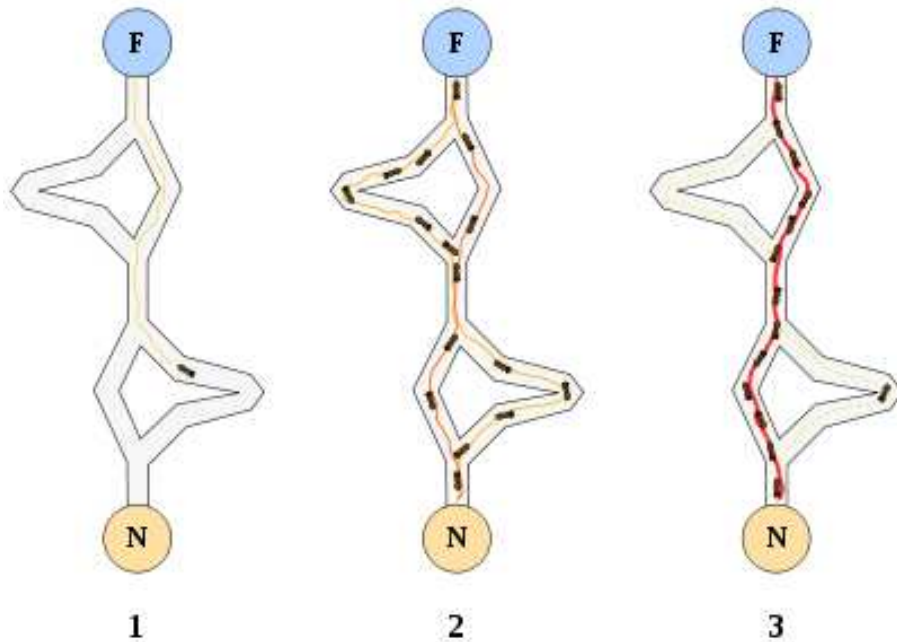
- Here, we use Minimum Weight Spanning Trees (MSTs), (Inbar et al., 2003)
- ... with an ant colony particle swarm optimisation (PSO) search algorithm

# Minimum Energy Spanning Trees



- Here, we have  $N = 5$  proteins and  $K = N(N-1)/2 = 10$  “edges”
- Each edge should consider many (e.g.  $P = 100$ ) docking solutions
- Naive enumeration would give  $P^{N(N-1)/2}$  possible combinations
- A spanning tree visits each node just once...
- ... there are only  $P^{N-1}N^{N-2}$  distinct spanning trees
- ... and when  $N < P$ , we get  $P^{N-1}N^{N-2} \ll P^{N(N-1)/2}$
- Strategy: search for the minimum energy spanning tree ...
- Getting technical: this is an “edge-weighted K-cardinality” problem...

# Multi-Component Docking using Ant-Colony Optimisation



Ant colony optimisation is based on the behaviour of real ants

When an ant finds food, it leaves a trail of pheromones

Other ants follow strong pheromones trails to reach the food quickly

- Here, we use 10 ants in parallel for 1,000 iterations...
- Each ant is assigned to a randomly generated spanning tree
- It must detect and score steric clashes, and update its trail
- It then makes a new spanning tree using the latest pheromone trails...

# MDOCK – Multi-Component Docking Results

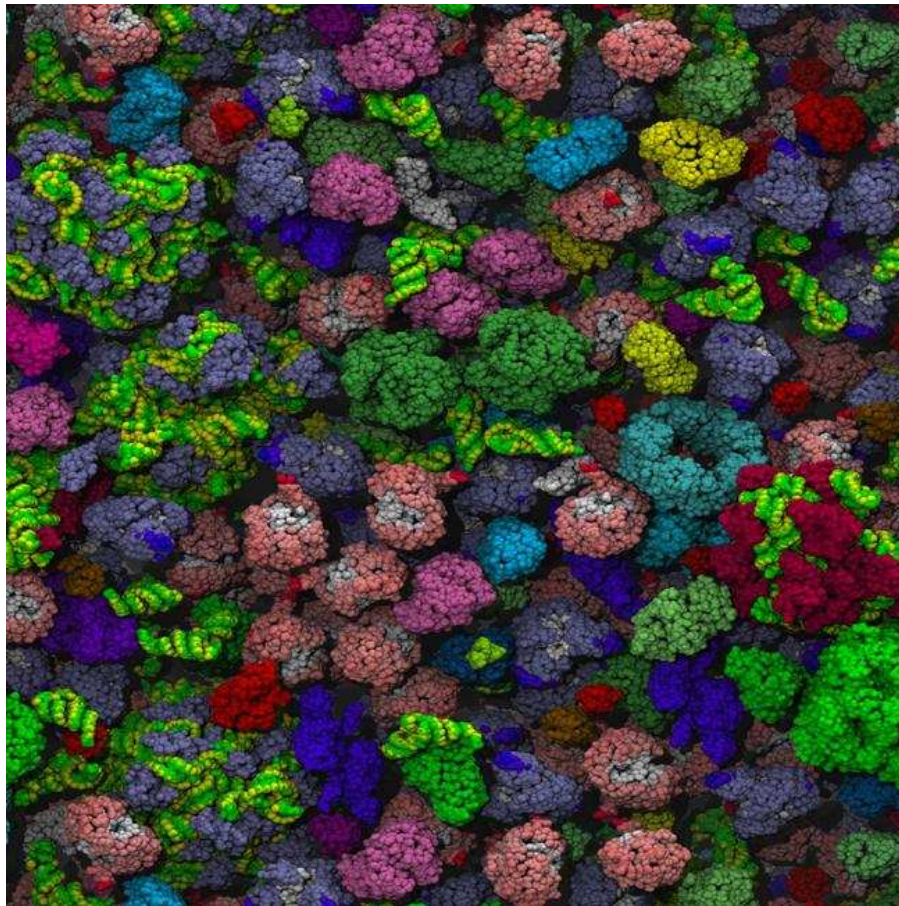
- There are not many multi-component examples in the PDB
- Therefore, several ‘targets’ were made from the same complex...
- 1VCB = von Hippel-Lindau ElonginC-ElonginB tumor suppressor protein
- 1IKN = Transcription factor I-kappa-B-alpha / NF-kappa-B
- 1K8K = Bovine actin polymerisation initiation complex Arp2 / Arp3

| Target | Chains        | Time (min) | Rank | RMSD (Å) | Best RMSD (Å) |
|--------|---------------|------------|------|----------|---------------|
| 1VCB   | A,B,C         | 43.8       | 1    | 0.58     | 0.58          |
| 1IKN   | A,C,D         | 77.3       | 1    | 9.17     | 0.88          |
| 1K8K   | A,B,D,E       | 123.5      | 1    | 4.96     | 2.19          |
| 1K8K   | A,B,D,E,F     | 168.6      | 2    | 9.48     | 2.99          |
| 1K8K   | A,B,D,E,F,G   | 194.1      | 15   | 4.63     | 3.53          |
| 1K8K   | A,B,C,D,E,F,G | 366.9      | –    | –        | 10.21         |

- Mostly good results, but why did we miss one?
- However, it would be very expensive to apply this algorithm to blind docking ...

# The Inside of a Cell is Highly Crowded

- This image shows a model of the cytoplasm in E. Coli

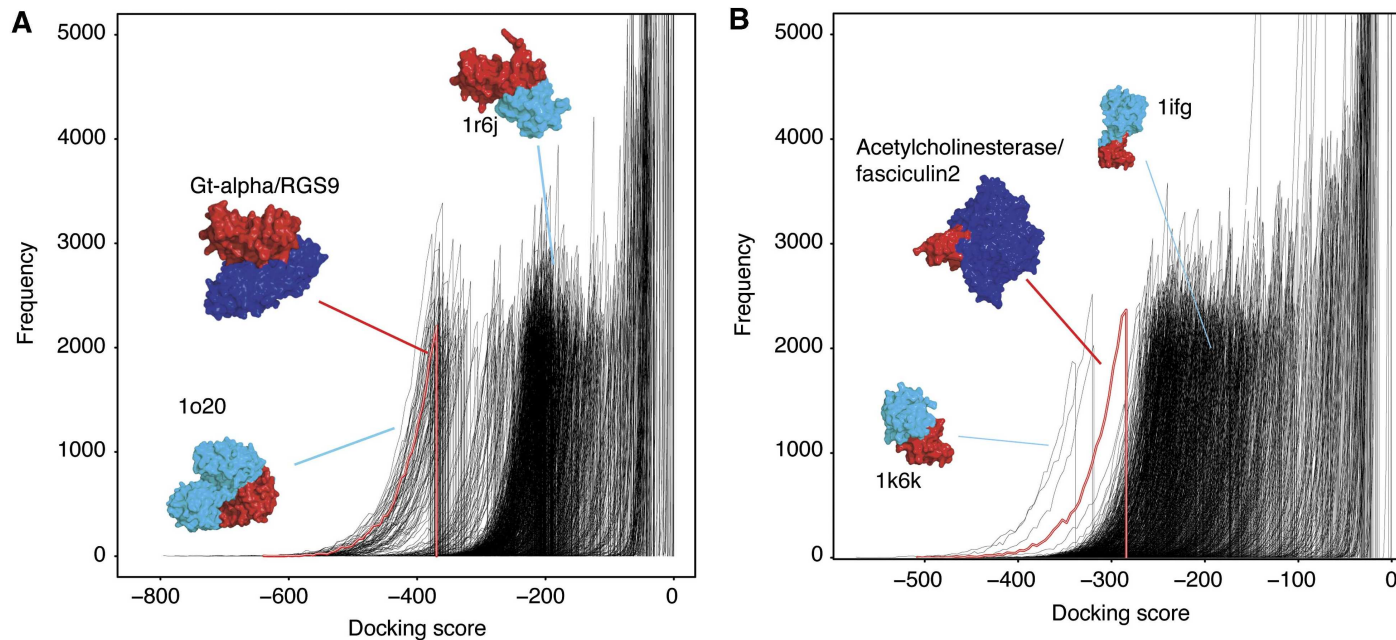


- Can we use docking algorithms to predict the protein-protein interactions ?

[McGuffee, Elcock \(2009\), PLoS Comp Biol, 6, e1000694](#)

# Large-Scale Cross-Docking Has Only Recently Become Feasible

- Wass et al. used Hex to cross-dock 56 true protein pairs with 922 non-redundant “decoys”
  - For each pair, they plotted the profile of the best 20,000 docking scores...



(negative scores are good; red/blue = correct PPI; red/cyan = incorrect interactions)

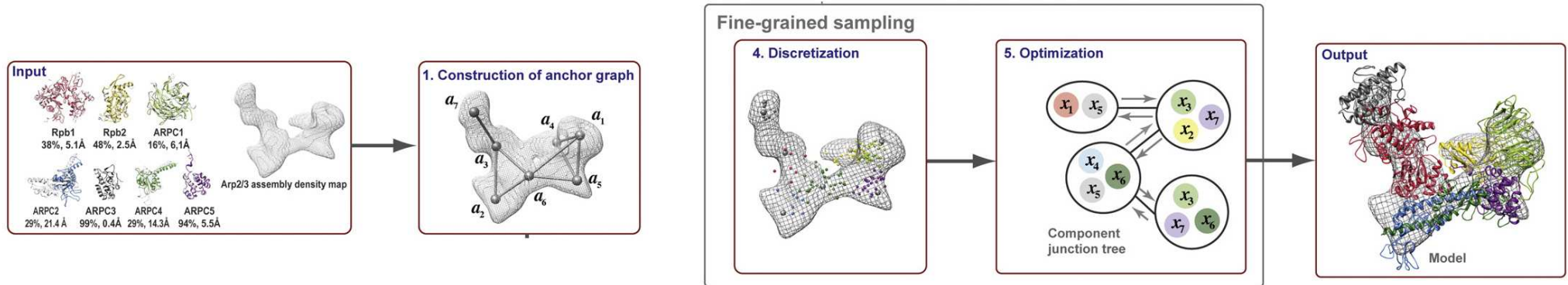
- 48/56 true PPIs have significantly (statistically) higher energies than background false pairs
- Only 8/56 true PPIs have indistinguishable profiles to the non-binders
- NB. this experiment is detecting energy funnels, not necessarily the correct docking pose

Wass et al. (2011) *Molecular Systems Biology*, 7, article 469



# IMP – Integrative Modeling Platform

- Python-based system for integrative multi-component modeling – <http://salilab.org/imp/>



- Combines structural data from: cryoEM (mainly), X-Ray, NMR, SAXS, Modeller, ...  
... with interaction data from BioGRID – <http://thebiogrid.org/>

- The overall approach is to maximise a multi-term objective function:

$$F = \sum_i \alpha_i + \sum_{i < j} \beta_{ij}$$

$\alpha_i$  are single-body terms (e.g. goodness of fit in a density map, protrusion penalty)

$\beta_{ij}$  are two-body terms (e.g. the docking score for two proteins in contact)

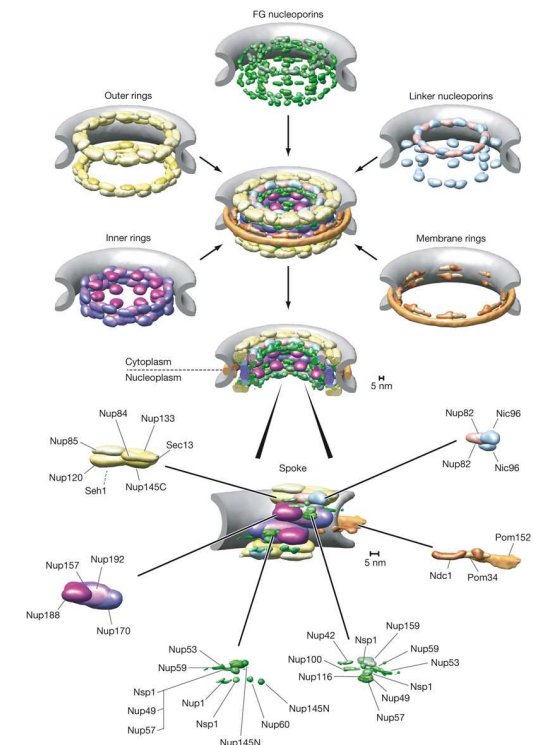
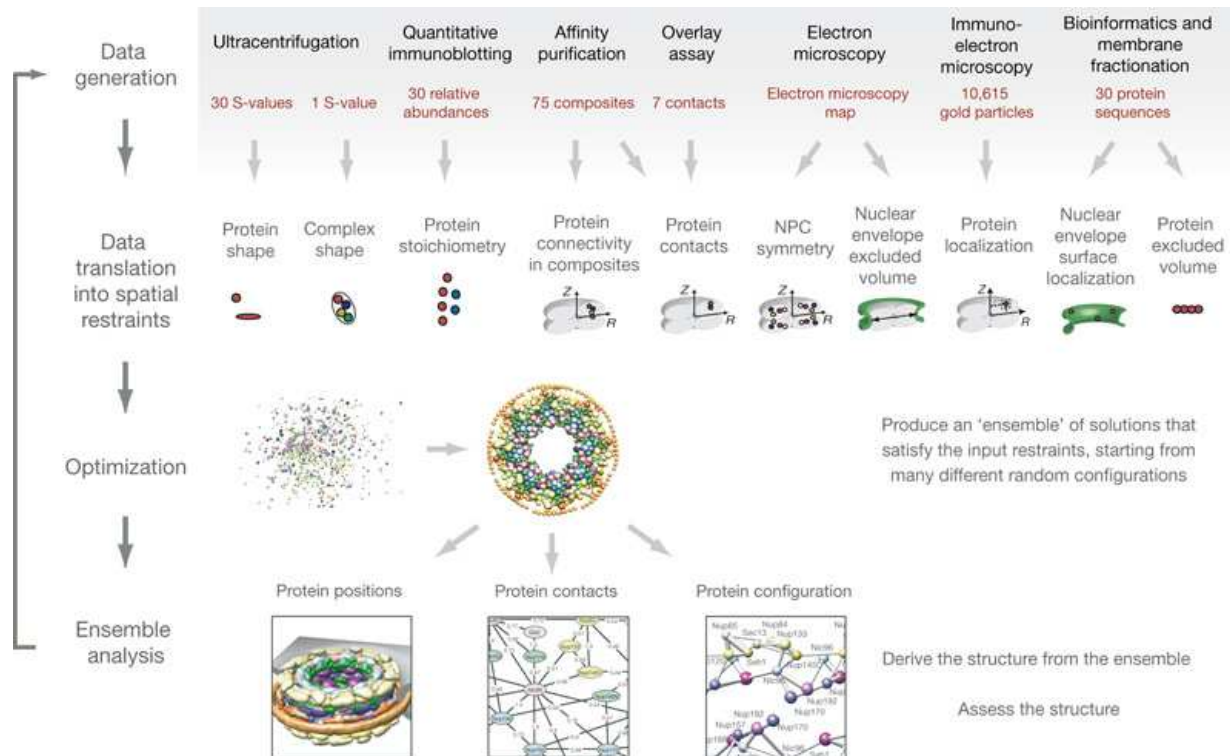
- But it is a **\*highly\*** combinatorial search space, with missing/incomplete data...

Russel et al. (2012) PLoS Biology, 10, e1001244

Lasker et al. (2009) J Molecular Biology, 388, 180–194

# Putting The Pieces Together – The Nuclear Pore Complex

- The NPC has some 650 components – raw data at <http://salilab.org/npc>

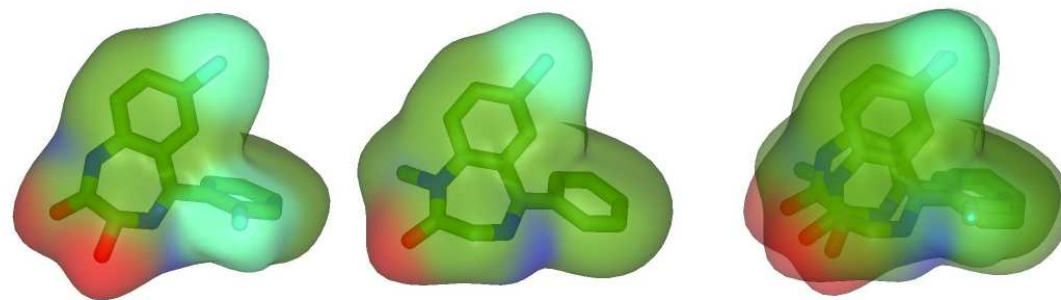


- It required an immense multi-disciplinary effort to build this model ...
- See Dreyfuss et al. for an interesting computational validation of the model

Alber et al. *Nature* (2007) 450, 683–694 and 695–701

Dreyfuss et al. *Proteins* (2012) – <http://dx.doi.org/10.1002/prot.24092>

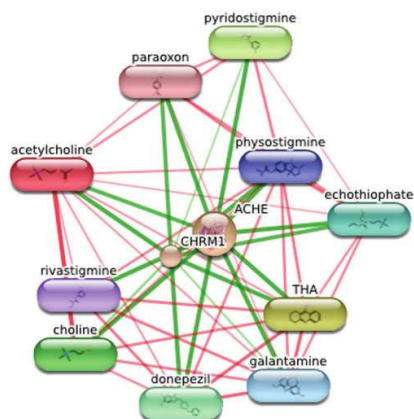
**But What About the Virtual Screening ?**



# Protein-Drug Interaction Resources

“The availability of interaction data between small molecule drugs and protein targets has increased substantially in recent years... We assembled a total of 4,767 unique interactions between 802 drugs and 480 targets, which means that on average every drug interacts with at least 6 targets...” [Mestres et al., \(2009\)](#).

- **STITCH** – Search Tool for Interactions of Chemicals – <http://stitch.embl.de>
  - 68,000 chemicals (including 2,200 drugs) linked to 1.5 million genes
- **ChEMBL** – database of drug-like bioactive molecules – <https://www.ebi.ac.uk/chembl/db/>
  - Binding & toxicity data for 1.1 million compounds and 5,200 protein targets



ChEMBL Bioactivity Search Results: 9071

| Parent | Ingestant | Bioactivity | Activity Comment | Operator | Value | Units | Assay ChEMBL ID | Assay Source          | Assay Type | Description   | ChEMBL Target ID | Target Name                           | Organism     | Target Mapping               | Curated By  | Reference   | Name % Reference |
|--------|-----------|-------------|------------------|----------|-------|-------|-----------------|-----------------------|------------|---|------------------|---------------------------------------|--------------|------------------------------|-------------|---|------------------|
|        |           | KI          |                  | =        | 19    | nM    | CHEMBL200198    | Scientific Literature | B          | Tested in vitro for antagonistic activity to displace [ <sup>3</sup> H]-PAF from rabbit platelet membrane PAF receptors | CHEMBL260        | Platelet activating factor receptor   | Homo sapiens | Homologous protein           | Expert      | <a href="#">Bioorg. Med. Chem. Lett., (1995) 5:23-263</a> | 11b              |
|        |           | KI          |                  | =        | 6     | nM    | CHEMBL260198    | Scientific Literature | B          | Tested in vitro for antagonistic activity to displace [ <sup>3</sup> H]-PAF from rabbit platelet membrane PAF receptors | CHEMBL260        | Platelet activating factor receptor   | Homo sapiens | Homologous protein           | Expert      | <a href="#">Bioorg. Med. Chem. Lett., (1995) 5:23-263</a> | 11c              |
|        |           | KI          |                  | =        | 10    | nM    | CHEMBL260198    | Scientific Literature | B          | Binding affinity for platelet activating factor receptor using [ <sup>3</sup> H]-PAF in rabbit platelet membranes       | CHEMBL260        | Platelet activating factor receptor   | Homo sapiens | Homologous protein           | Expert      | <a href="#">Bioorg. Med. Chem. Lett., (1995) 5:23-263</a> | 3                |
|        |           | IC50        |                  | =        | 1800  | nM    | CHEMBL640415    | Scientific Literature | B          | Binding affinity towards AMPA receptor using [ <sup>3</sup> H]-AMPA as radioligand                                      | CHEMBL392        | Glutamate receptor ionotropic, AMPA 1 | Mus musculus | Multiple homologous proteins | AutoCurator | <a href="#">Bioorg. Med. Chem. Lett., (1994) 5:2-371</a>  | 7                |

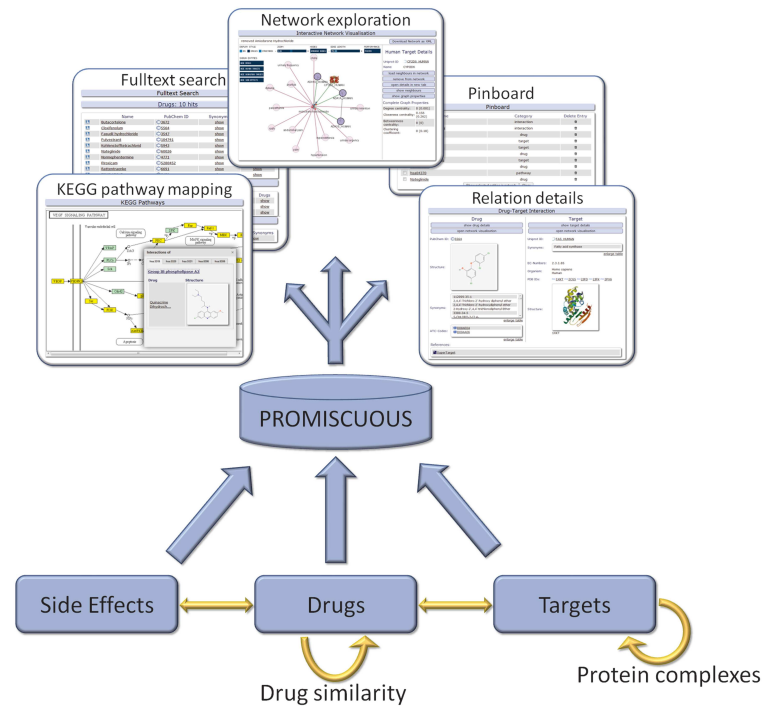
[Mestres et al. \(2009\) Molecular BioSystems, 5, 1051–1057](#)

[Kuhn et al. \(2008\) Nucleic Acids Research, 36, D684–D688 \(STITCH\)](#)

[Gaulton et al. \(2012\) Nucleic Acids Research, 40, D1100–D1107 \(ChEMBL\)](#)

# A Growing Interest in Drug Promiscuity and Drug Repositioning

- Approx 90% of new drugs fail to reach market – often due to toxicity or lack of efficacy  
toxicity – e.g. from unwanted off-target interactions  
lack of efficacy – e.g. from robustness of biological network
- Example – PROMISCUOUS – <http://bioinformatics.charite.de/promiscuous/>  
“network-based drug repositioning” – 25K drugs, 21K drug-protein, 104K PPIs

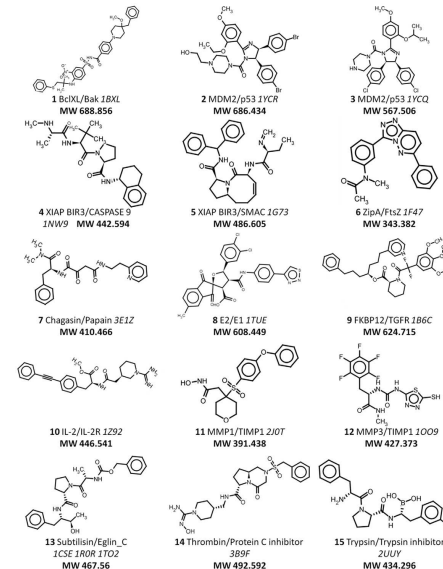
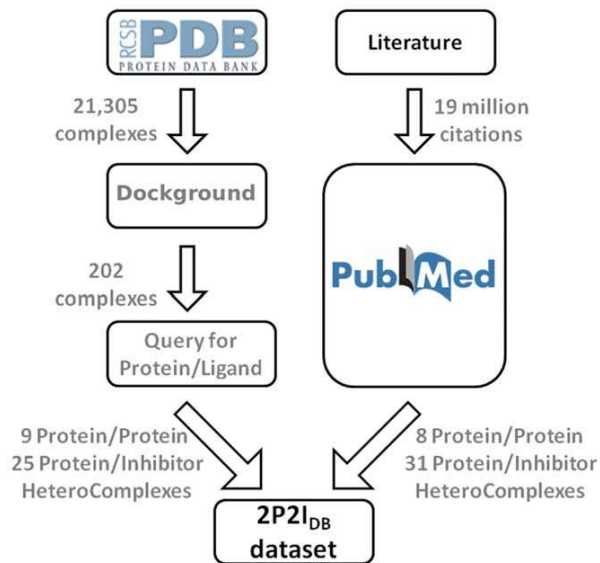


von Eichborn et al. (2011) *Nucleic Acids Research*, 39, D1060–D1066 (PROMISCUOUS)

Kuhn et al. (2011) *Molecular Systems Biology*, 6, 343 (SIDER)

# Atomic Resolution Studies of Hetero PPIs and Inhibitors

- TIMBAL – <http://www-cryst.bioc.cam.ac.uk/timbal/> – 27 structures, 104 small molecules
- 2P2I (= PPI inhibition) – <http://2p2idb.cnrs-mrs.fr/> – 17 PPIs, 56 small molecules



- The ligands generally have high MW and are hydrophobic
  - The PPIs have few/no small interface pockets; small conformational changes on binding
  - See also Dr. PIAS – <http://www.drpias.net/> – SVM-based prediction of druggable PPIs
- Higueruelo et al. (2009) Chemical Biology Drug Design, 74, 457–467 (TIMBAL)
- Borgeas et al. (2010) PLoS One, 4, e9598 (2P2I)
- Sugaya, Furuya (2011) BMC Bioinformatics, 12, 50 (Dr. PIAS)

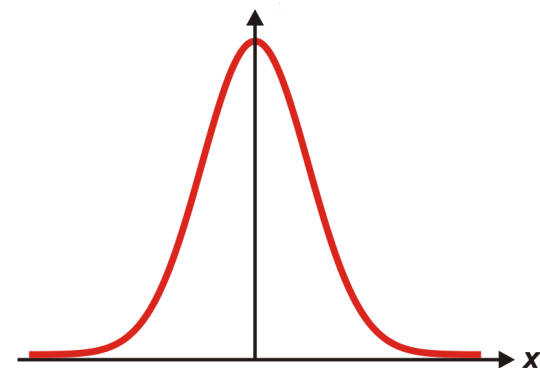
# A Gaussian Representation of Molecular Shape

- Represent each atom in a molecule as a 3D Gaussian density function:

$$\rho_i(r) = \beta e^{-\gamma r^2 / \sigma_i^2}$$

and choose  $\beta, \gamma$  such that:  $\int \rho_i(r) d\underline{x} = \frac{4}{3}\pi\sigma_i^3$

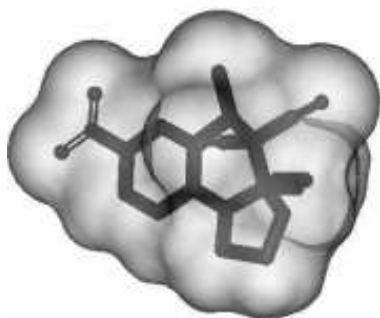
where  $\sigma_i$  = van der Waals radius of atom  $i$



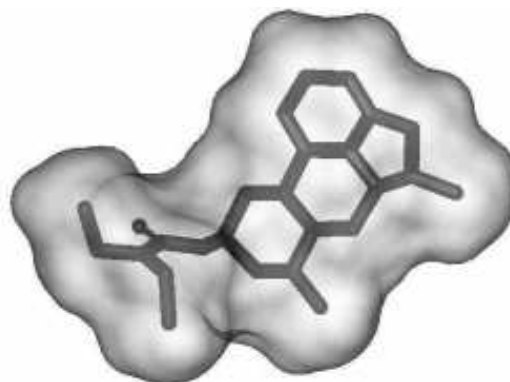
- Represent the “density” of a molecule as a sum of  $N$  atomic densities:

$$\begin{aligned} \rho &= \sum_{i < N} \rho_i - \sum_{i < j < N} \rho_i \rho_j + \sum_{i < j < k < N} \rho_i \rho_j \rho_k - \dots \\ &= 1 - \prod_{i=0}^{N-1} (1 - \rho_i) \end{aligned}$$

- Some examples:



HIFYOK



PEWHII



ABMQZD

# Gaussian Overlap Volumes and Tanimoto Scores

- The overlap volume between two atomic Gaussians is just another Gaussian:

$$\begin{aligned} V_{ij} &= \int \rho_i \rho_j d\underline{x} \\ &= \beta_i \beta_j \left( \frac{\pi}{\alpha_i + \alpha_j} \right)^{3/2} e^{-\left( \frac{\alpha_i \alpha_j}{\alpha_i + \alpha_j} \right) R_{ij}^2} \end{aligned}$$

where  $R_{ij}$  is distance between the atom centres, and  $\alpha_i = \gamma / \sigma_i^2$

- Hence the overlap volume between two molecules can also be calculated easily...

... and normalised to give a Tanimoto-like similarity score (with range  $0 < S_{AB} \leq 1.0$ ):

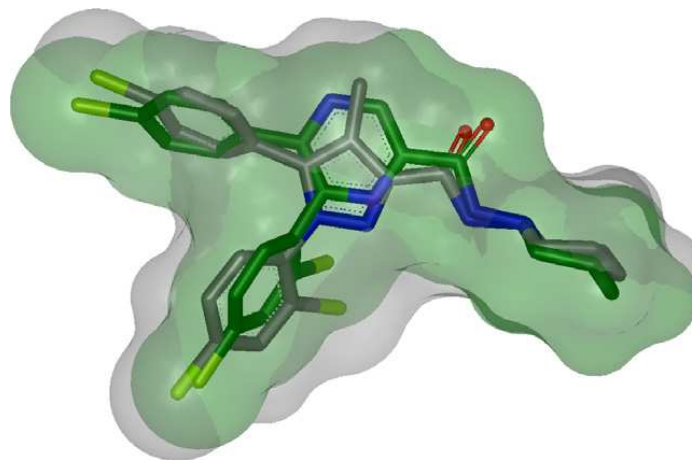
$$V_{AB} = \int \rho_A \rho_B d\underline{x}$$

$$S_{AB} = \frac{V_{AB}}{V_{AA} + V_{BB} - V_{AB}}$$

... and this is easy to optimise:

$$\frac{\delta V_{ij}}{\delta x} = -2 \left( \frac{\alpha_i \alpha_j}{\alpha_i + \alpha_j} \right) (\underline{x}_i - \underline{x}_j) V_{ij}$$

etc.





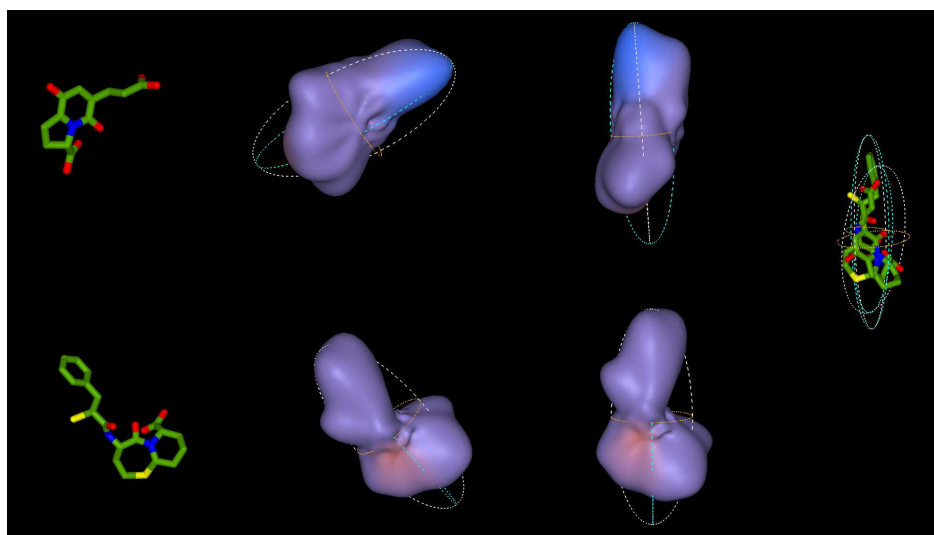
# ROCS – “Rapid Overlay of Chemical Structures”

- ROCS is a commercial implementation of the Gaussian representation of Grant et al.
- ROCS initially uses “steric multipoles” to align molecules with the Cartesian axes

$$M_{pq} = \int pq\rho d\underline{x}, \text{ where each } p \text{ and } q \text{ stands for } x, y, \text{ or } z$$

Diagonalising  $M$  is equivalent to finding the principal ellipsoidal axes...

- ROCS then maximises the Gaussian overlap starting from 4 different orientations (axis flips)



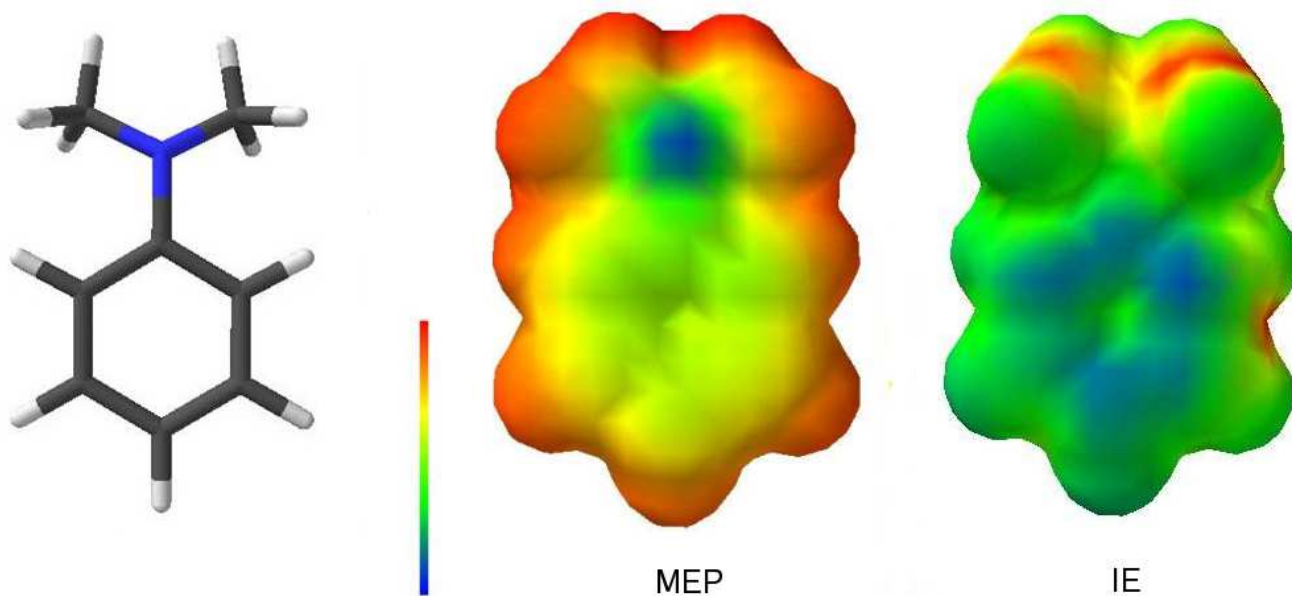
- Recently, “FASTROCS” (GPU-based version) – up to  $10^6$  superpositions/second !!

<http://www.eyesopen.com/rocs/>

Haque, Pande (2009), J Computational Chemistry, 31, 117–132 (open source GPU version)

# ParaSurf – SH Surfaces & Properties from Semi-Empirical QM

- From MOPAC or VAMP calculate:
  - Density contours of  $2 \times 10^{-4} e/\text{\AA}^3$  ( $\sim$  SAS)
  - Key local properties: MEP,  $IE_L$ ,  $EA_L$ ,  $\alpha_L$
- Encode as SH expansions to  $L=15$ :  $f(\theta, \phi) = \sum_{l=0}^L \sum_{m=-l}^l f_{lm} y_{lm}(\theta, \phi)$



Lin, Clark (2005), *J Chemical Information & Modeling*, 45, 1010–1016

Clark (2004), *J Molecular Graphics*, 22, 519–525

# ParaFit – High Throughput SH Surface & Property Matching

Distance:  $D = \int (r_A(\theta, \phi) - r_B(\theta, \phi)')^2 d\Omega$  (in units of area)

Orthogonality:  $D = |\underline{a}|^2 + |\underline{b}|^2 - 2\underline{a} \cdot \underline{b}'$

Rotation:  $b'_{lm} = \sum_{m'} R_{mm'}^{(l)}(\alpha, \beta, \gamma) b_{lm'}$

Hodgkin:  $S = 2\underline{a} \cdot \underline{b}' / (|\underline{a}|^2 + |\underline{b}|^2)$

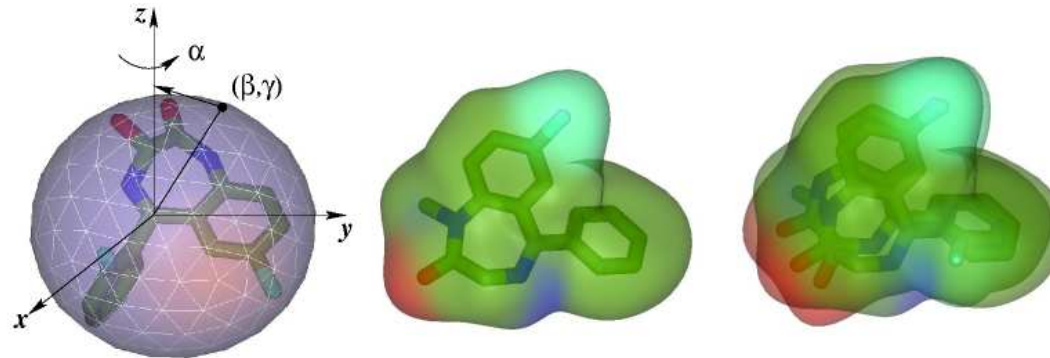
Carbo:  $S = \underline{a} \cdot \underline{b}' / (|\underline{a}| \cdot |\underline{b}|)$

Tanimoto:  $S = \underline{a} \cdot \underline{b}' / (|\underline{a}|^2 + |\underline{b}|^2 - \underline{a} \cdot \underline{b}')$

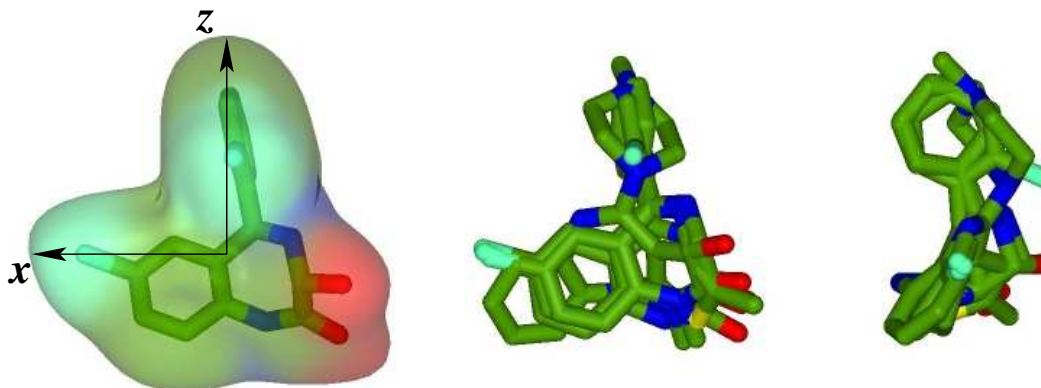
Multi-property:  $S = pS^{\text{shape}} + qS^{\text{MEP}} + rS^{\text{IE}_L} + sS^{\text{EA}_L} + tS^{\alpha_L}$

# Brute-Force Spherical Harmonic Surface Superpositions

- Generate 22,500 Euler rotations from icosahedral tessellation of sphere



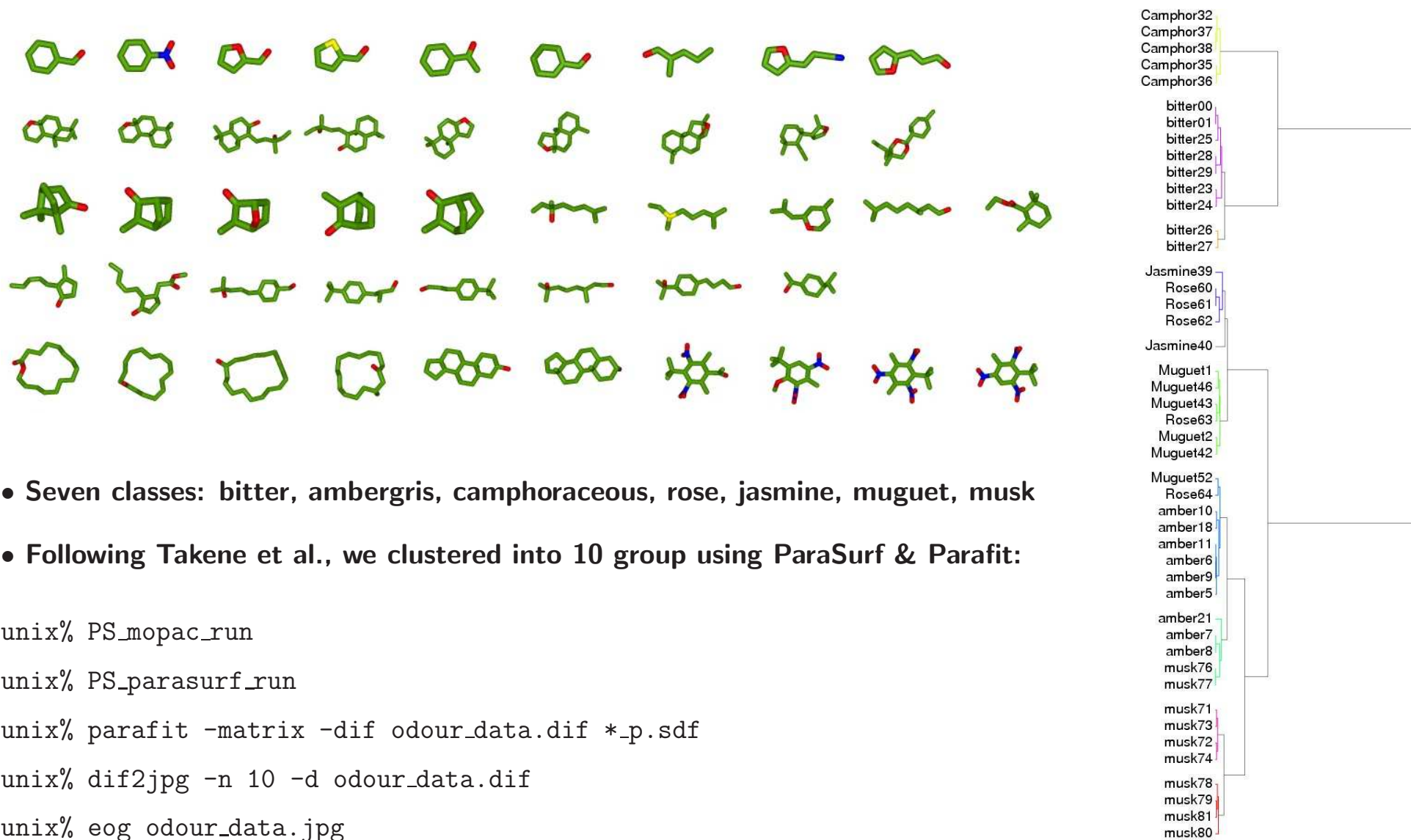
- Refine with  $16 \times 16 \times 16$  grid of 1 degree steps (gives about 50 molecules / second)
- Can also pre-process a set of molecules by aligning them to the principal axes



- Pre-aligned “canonical” orientations of similar molecules often overlay very well ...

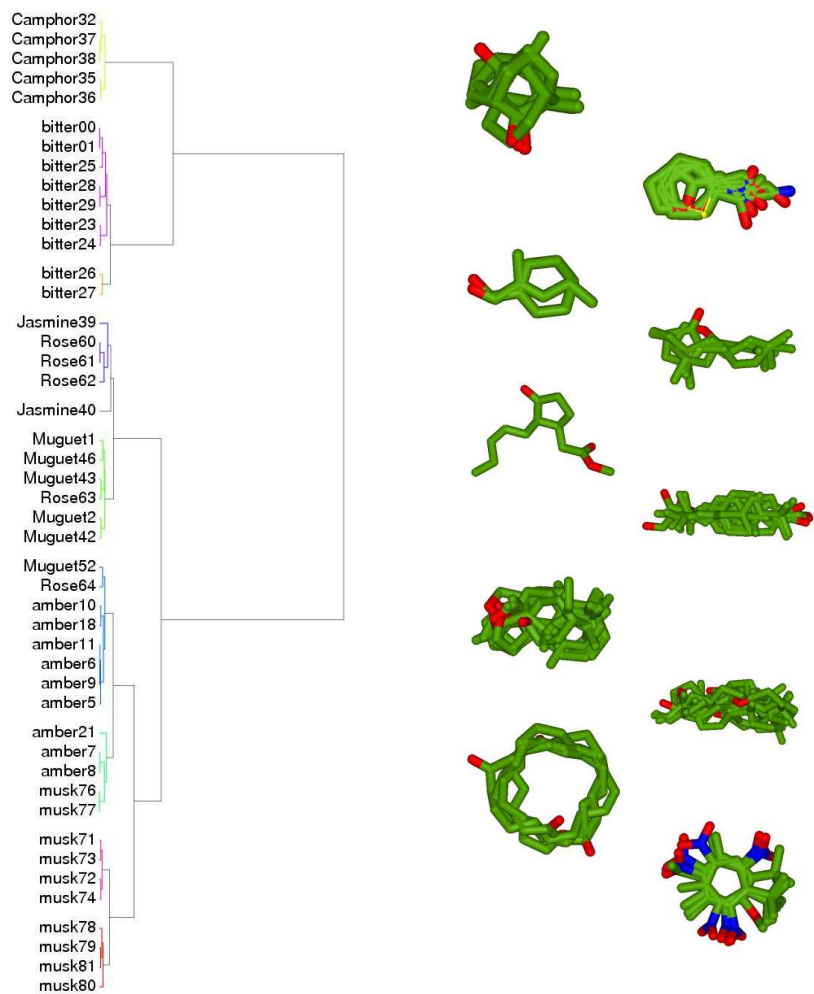
# Clustering the Odour Dataset using 2D SH Surface Shapes

(Takane et al. (2004) Org. Biomol. Chem. 2 3250–3255)



# Visualising The Odour Dataset Clustering Results

## Clustering Superposed Pairs

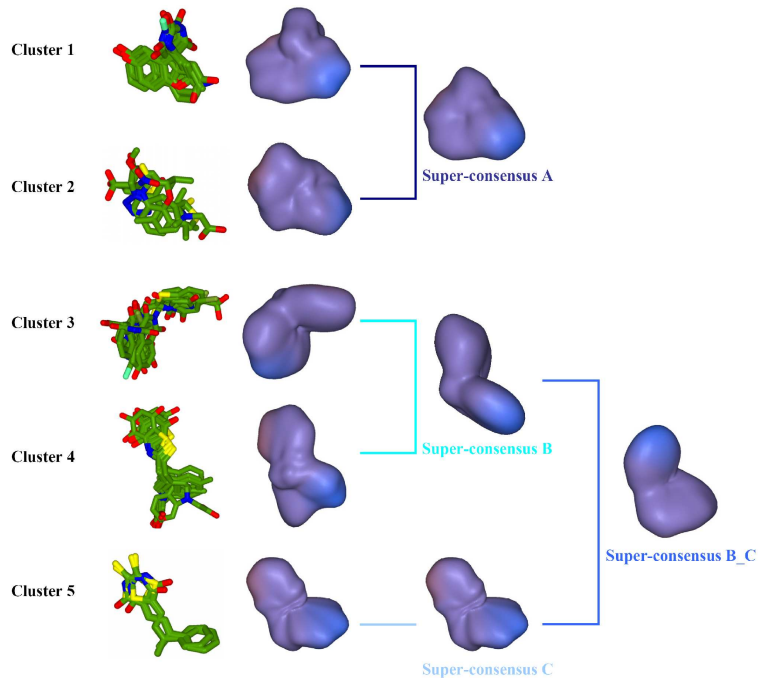


## Clustering Canonical Orientations



# Promiscuous Protein Targets Seem to be Rather Common

- Example: ALR2 is known to bind at least 5 different ligand scaffold families...



- Several other promiscuous targets in the literature:

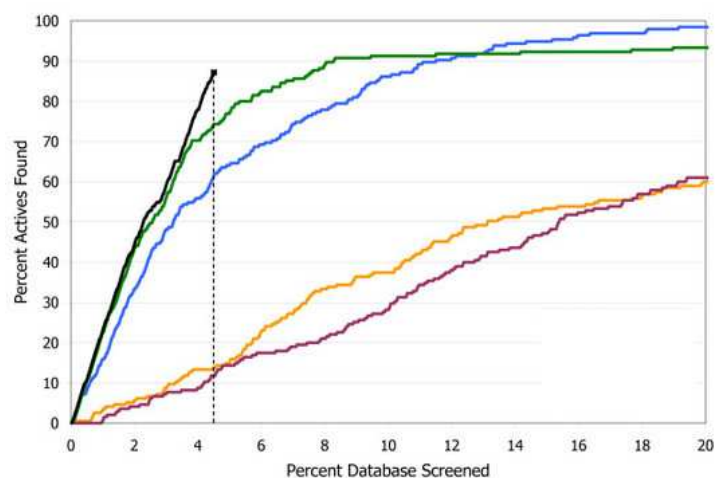
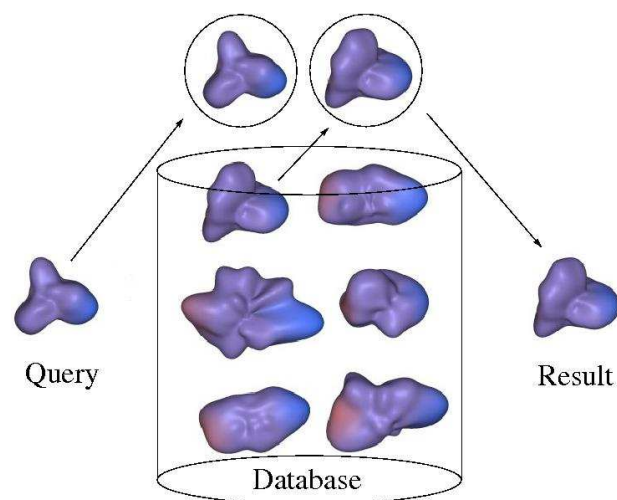
- the  $\alpha 1\beta 1$  and  $\alpha 2\beta 1$  integrins,
- factor H, LRP6, PPAR- $\gamma$ , LXR- $\beta$ ,
- ACHE, P38, FXA, VEGFR2, PXR,
- $\beta$ -secretase, thrombin, CDK2,
- LAIR-1, LAIR-2, LTBLP-2, NS2B-NS3.

- For ligand-based virtual screening, these examples suggest:

- cluster the 3D shapes of any known ligands before performing VS ...
- compare shape-based VS performance with and without clustering ...
- ... any large differences could suggest a promiscuous (multi-site?) substrate.

# Ligand-Based VS (LBVS) Principals

- LBVS aims to find new actives by similarity to one or more existing actives
- Usually LBVS has two phases – retrospective (i.e. “training mode”), and prospective
- Main purpose of retrospective VS is to find the best algorithm + query (molecule/conformation)
  - Prerequisites: some know actives + a good set of decoys (similar mol wt, chemistry)
- Historically, enrichment plots have been popular for analysing ranked lists of VS results



- **Disadvantages:**

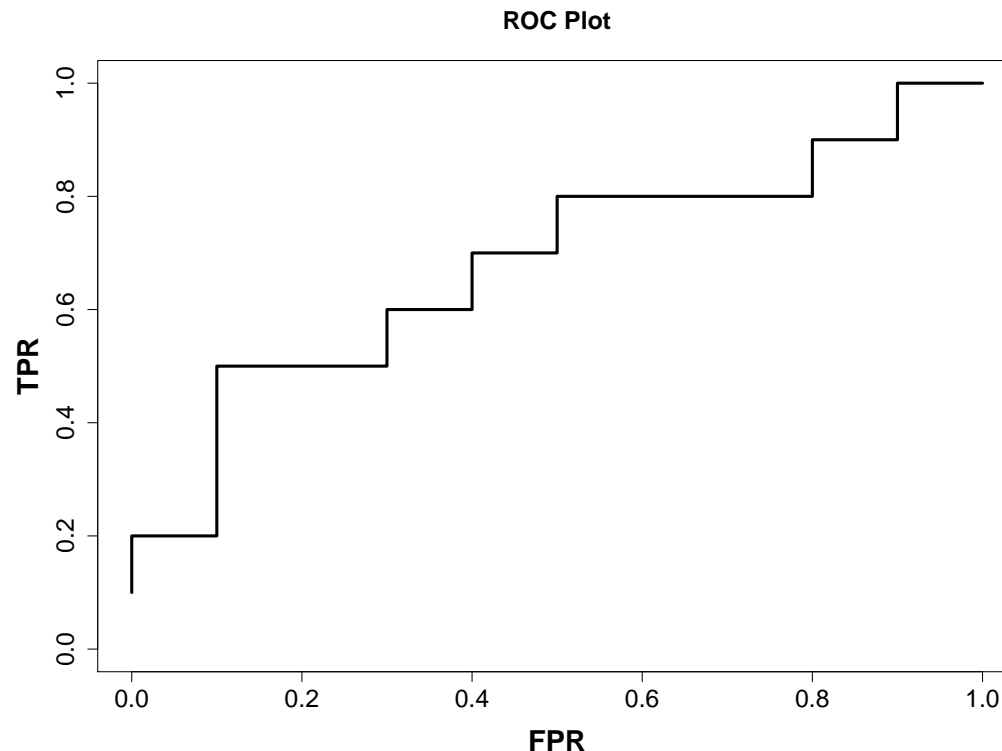
- enrichment plots (or enrichment factors) depend on the no. of actives
- it is difficult to compare different enrichment plots



# Receiver-Operator-Characteristic (ROC) Plots

- ROC plots show the ability of a classifier to distinguish positive and negative instances
  - A ROC plot shows the true positive rate (TPR) against the false positive rate (FPR)
  - Suppose 10 positive and 10 negative instances have been scored by a classifier...

| Score | Class | Npos | Nneg | TPR | FPR |
|-------|-------|------|------|-----|-----|
| 0.90  | pos   | 1    | 0    | 0.1 | 0.0 |
| 0.80  | pos   | 2    | 0    | 0.2 | 0.0 |
| 0.70  | neg   | 2    | 1    | 0.2 | 0.1 |
| 0.60  | pos   | 3    | 1    | 0.3 | 0.1 |
| 0.55  | pos   | 4    | 1    | 0.4 | 0.1 |
| 0.54  | pos   | 5    | 1    | 0.5 | 0.1 |
| 0.53  | neg   | 5    | 2    | 0.5 | 0.2 |
| 0.52  | neg   | 5    | 3    | 0.5 | 0.3 |
| 0.51  | pos   | 6    | 3    | 0.6 | 0.3 |
| 0.50  | neg   | 6    | 4    | 0.6 | 0.4 |
| 0.40  | pos   | 7    | 4    | 0.7 | 0.4 |
| 0.39  | neg   | 7    | 5    | 0.7 | 0.5 |
| 0.38  | pos   | 8    | 5    | 0.8 | 0.5 |
| 0.37  | neg   | 8    | 6    | 0.8 | 0.6 |
| 0.36  | neg   | 8    | 7    | 0.8 | 0.7 |
| 0.35  | neg   | 8    | 8    | 0.8 | 0.8 |
| 0.34  | pos   | 9    | 8    | 0.9 | 0.8 |
| 0.33  | neg   | 9    | 9    | 0.9 | 0.9 |
| 0.32  | pos   | 10   | 9    | 1.0 | 0.9 |
| 0.31  | neg   | 10   | 10   | 1.0 | 1.0 |



- The area under the curve (AUC) gives a good overall measure of classifier performance
- A random classifier gives a diagonal line:  $TPR=FPR$  (AUC=0.5)
- A perfect classifier gives  $TPR=1.0$  for all FPR (AUC=1.0)

## Several Other Common VS Quality Measures

- Suppose there are  $n$  actives in a total of  $N$  molecules, and the scoring function is used to produce a ranked list of molecules:  $i = 1, 2, 3, \dots, N$ .
- Often we are most interested in the quality of the top (e.g. top 1%) of the ranked list

- Enrichment Factor: 
$$EF_{x\%} = \frac{n_a/N_{x\%}}{n/N}$$

- ROC AUC: 
$$AUC = \frac{1}{n} \sum_{i=1}^n (1 - f_i)$$

- ROC  $AUC_{x\%}$  : 
$$AUC_{x\%} = \text{calculate graphically}$$

- Balanced ROC: 
$$BAROC = \frac{1}{n} \sum_{i=1}^n e^{-\alpha f_i}$$

- Sum of Logs of Rank: 
$$SLR = - \sum_{i=1}^n \log\left(\frac{r_i}{N}\right)$$

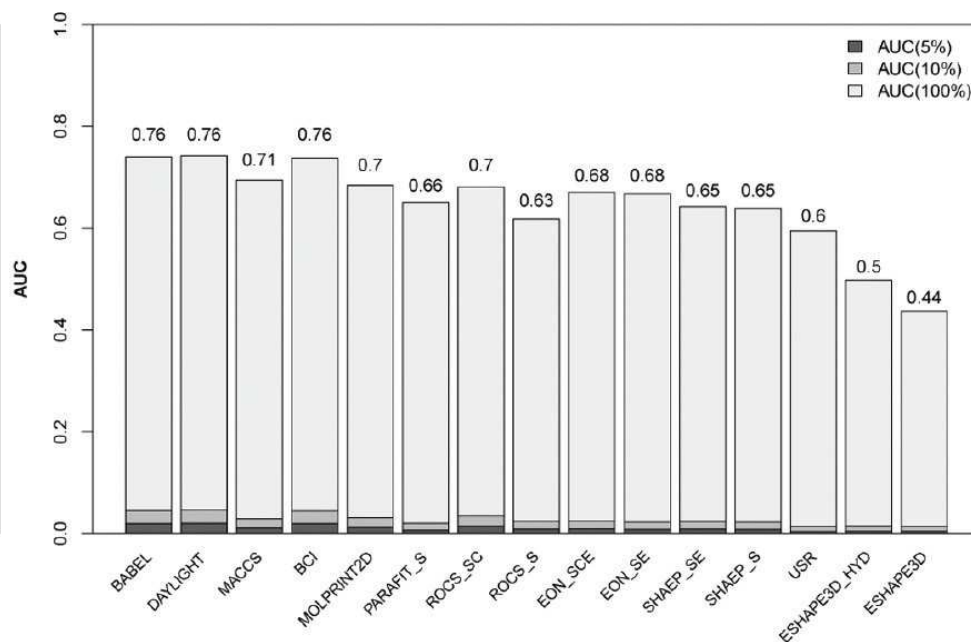
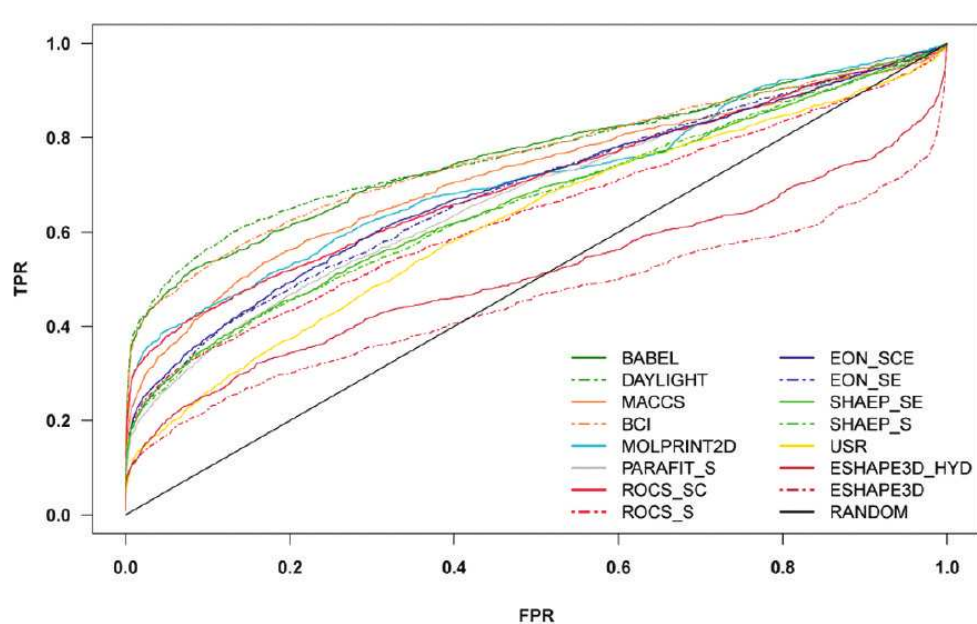
- Normalised SLR: 
$$NSLR = \sum_{i=1}^n \log\left(\frac{r_i}{N}\right) / \sum_{i=1}^n \log\left(\frac{i}{N}\right)$$

(here, the top  $x\%$  of the list contains  $N_{x\%}$  molecules and  $n_a$  actives,  $r_i$  is the rank of the  $i^{\text{th}}$  active, and  $f_i$  is the fraction of inactives ranked higher than  $i$ )

- Which is best? Debatable! These days, ROC AUC,  $AUC_{5\%}$ ,  $AUC_{10\%}$  are quite popular...

# Comparing Ligand-Based Virtual Screening Methods

- We calculated aggregate ROC plots to compare several VS methods on the “DUD” dataset
  - DUD = Directory of Useful Decoys – <http://dud.docking.org/> – 40 targets, 100K decoys
  - 2D methods = Babel, Daylight, MACCS, MCI, Molprint2D
  - 3D methods = Parafit, ROCS, SHAEP, USR, Eshape3D



- The fingerprint methods perform remarkably well (!)
- Suggests need to improve 3D methods – better query conformations ? shape clustering ?

# Conclusions

- Modeling flexibility during docking is still a major challenge
- Cross-docking can detect protein-protein partners remarkably often
- Knowledge-based protein docking is becoming increasingly useful
- Most Pfam families have just one binding site – often re-used
- Several proteins bind multiple ligand families – promiscuous targets
- Fast 3D virtual screening algorithms are becoming available
- All-vs-all 3D protein docking and ligand shape-matching now feasible ?
- Choosing a good query conformation still a challenge in ligand-based VS

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